# Chapter 1: MOS Devices and Circuits

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#### Sections:

The MOS Transistor - - - The Basic Inverter - - - Inverter Delay - - - Parasitic Effects - - - Driving Large Capacitive Loads - - - Space vs Time - - - Basic NAND and NOR Logic Circuits - - - Super Buffers - - - A Closer Look at the Electrical Parameters - - - Depletion Mode vs Enhancement Mode Pullups - - - Delays in Another Form of Logic Circuitry - - - Pullup/Pulldown Ratios for Inverting Logic Coupled by Pass Transistors - - - Properties of Cross Coupled Circuits - - - Effects of Scaling Down the Dimensions of MOS Circuits and Systems

In this chapter we begin with a discussion of the basic properties of the n-channel MOS field effect transistor (MOSFET). We then describe and analyze a number of circuits composed of interconnected MOS transistors. The circuits described are typical of those we will commonly use in the design of LSI systems. The analysis, though highly condensed, is conceptually correct and provides a basis for the solution of most system problems typically encountered.

Integrated systems in nMOS technology contain three levels of conducting material separated by intervening layers of insulating material. Proceeding from top to bottom, these levels are termed the *metal*, the *polysilicon*, and the *diffusion* levels respectively. Patterns for paths on these three levels, and the locations of contact cuts through the insulating material to connect certain points between levels, are transferred into the levels during the fabrication process from *masks* similar to photographic negatives. The details of the fabrication process will be discussed in chapter 2.

In the absence of contact cuts through the insulating material, paths on the metal level may cross over paths on the polysilicon or diffusion levels with no significant functional effect. However, wherever a path on the polysilicon level crosses a path on the diffusion level, a transistor is created. Such a transistor has the characteristics of a simple switch, with a voltage on the polysilicon level path controlling the flow of current in the diffusion level path. Circuits composed of such transistors, interconnected by patterned paths on the three levels, form our basic building blocks. With these basic circuits, we will architect LSI systems, to be fabricated on the surface of monolithic crystalline chips of silicon.

## The MOS Transistor

An MOS transistor will be produced on the integrated system chip wherever a polysilicon path crosses a diffusion path, as shown in figure 1a. The electrical symbol used to represent the MOS transistor in our circuit diagrams is shown in figure 1b, along with symbols and polarities of certain voltages of interest. Note that the source and drain terminals of the device are physically symmetrical. In practice these terminal labels are assigned such that  $V_{\rm ds}$  is normally positive. A more detailed view of the rectangular region called the gate, where the polysilicon (poly) crosses the diffusion, is given in figure 1c. During fabrication the diffusion paths are formed after the poly paths are formed. The poly gate and thin layer of oxide under it masks the region under the gate during diffusion, and there is no direct diffusion connection between the source and drain terminals of the transistor.

In the absence of any charge on the gate, the drain to source path through the transistor is like an open switch. The gate, separated from the substrate by the layer of thin oxide, forms a capacitor. If sufficient positive charge is placed on the gate so that  $V_{\rm gs}$  exceeds a threshold voltage  $V_{\rm th}$ , electrons will be attracted to the region under the gate to form a conducting path between drain and source. Most of the transistors we will use in our systems have threshold voltages greater than zero. These are called enhancement mode MOSFETs, and their threshold voltage typically equals  $\sim 0.2 (\text{VDD})$ , where VDD is the positive supply voltage for the particular technology.

The basic operation performed by the MOS transistor is to use charge on its gate to control the movement of negative charge between source and drain through the channel under the gate. The current from source to drain equals the charge induced in the channel divided by the transit time or average time that a packet of negative charge requires to move from source to drain. The transit time itself is the distance the charge has to move divided by its average velocity. In semiconductors under normal conditions, the velocity is proportional to the electric field driving the charge carriers. The relationship between drain to source current  $I_{ds}$ , drain to source voltage  $V_{ds}$ , and gate to source voltage  $V_{gs}$  is sketched in figure 1d. In a common mode of MOS transistor operation called saturation, the average electric field E in the channel is proportional to the difference between  $V_{gs}$  and  $V_{th}$ , and is not a function of  $V_{ds}$ . This is the region in fig.1d where the  $I_{ds}$  lines, plotted at constant  $V_{gs}$ , run horizontally. In saturation, the transit time is given by eq. 1.

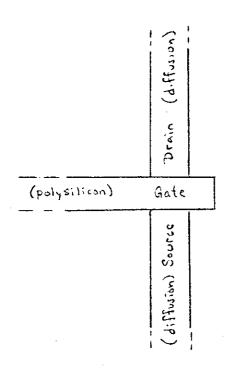


Fig. 1 a. Mos TRANSISTOR (TOP VIEW)

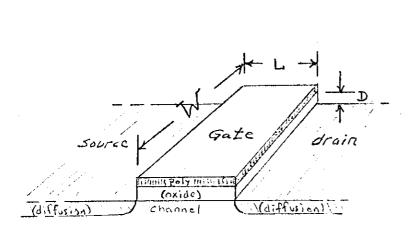


Fig. 1 C. MOSFET GATE DIMENSIONS

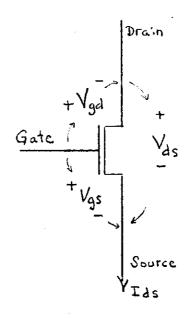


Fig. 1 b. Mos TRANSISTOR SYMBOL (Subscripts in "plus to minus direction" sequence)

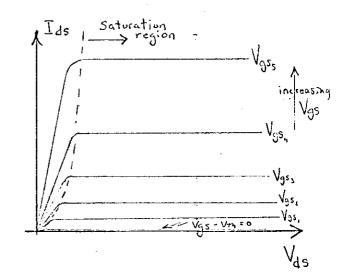


Fig. Ld. CURRENT US VOLTAGE

Transit time:

$$\tau = L/\text{velocity} = 2L/\mu E = 2L^2/[\mu(V_{gs} - V_{th})]$$
 [eq.1]

The proportionality constant  $\mu$  is called the *mobility* of the charge carriers, in this case electrons, under the influence of an electric field in the conducting material of the channel region. It is a velocity per unit electric field (cm<sup>2</sup>/volt-sec). The factor of 2 arises because of the non-uniformity of the electric field in the channel region<sup>1</sup>. We shall see that the transit time is the fundamental time unit of the entire integrated system.

The amount of negative charge in transit is just the gate capacitance times the voltage on the gate in excess of the threshold voltage. The capacitance of two parallel conductors of area A, separated by insulating material of thickness d, equals  $\varepsilon A/d$ . The proportionality constant  $\varepsilon$  is called the permittivity of the insulating material, and has a simple interpretation. It is the capacitance of parallel conductors of area  $A = 1 \text{ cm}^2$ , separated by a thickness d = 1 cm of the insulator material, and is in the units farad/cm. Therefore, the gate capacitance equals  $\varepsilon WL/D$ . Thus the charge in transit is given by eq. 2, and the current is given by eq. 3.

Charge in transit:

$$Q = -C_g(V_{gs} - V_{th}) = -\frac{\epsilon WL}{D}(V_{gs} - V_{th})$$
 [eq.2]

Current:

$$I_{ds} = -I_{sd} = -\frac{\text{charge in transit}}{\text{transit time}} = \frac{\mu \epsilon W(V_{gs} - V_{th})^2}{2LD}$$
 [eq.3]

Note that in eq. 1, the entire drain to source voltage was not available for reducing the transit time. Drain voltage in excess of one threshold below the gate voltage creates a short, high electric field region adjacent to the drain which the carriers cross very quickly. However, the electric field in the major portion of the channel from the source up to this point is proportional to  $V_{\rm gs}$  -  $V_{\rm th}$ , as shown in figure 1e.

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Although the above equations are greatly simplified, they provide sufficient information to make many design decisions with which we will be faced, and also give us insight into the scaling of devices to smaller sizes. In particular, the transit time  $\tau$  can be viewed as the basic time unit of any system we shall build in the integrated technology. In almost all situations, the fastest operation which we can perform is to transfer a signal from the gate of one MOS transistor onto the gate of another. In the absence of stray capacitance, the transit time is the minimum time in which one transistor can transfer a charge from its gate onto the gate of the subsequent transistor. For example, to transfer a charge from one transistor onto two transistors identical to it requires a minimum of two transit times. Thus, the transit time of the basic transistor in an integrated system can be viewed as the unit of time in which all other times in the system are scaled.

### The Basic Inverter

The first logic circuit we will describe is the basic digital inverter. Analysis of this circuit is then easily extended to analysis of basic NAND and NOR logic gates. The inverter's logic function is to produce an output which is the complement of its input. When describing the logic function of circuits in LSI systems, we assign the value logic-1 to voltages equaling or exceeding some defined logic threshold voltage, and logic-0 to voltages less than this threshold voltage.

Were there an efficient way to implement resistors in the MOS technology, we could build a basic digital inverter circuit using the configuration of figure 2a. Here, if the inverter input voltage  $V_{in}$  is less than the transistor threshold voltage  $V_{th}$ , then the transistor is switched off, and  $V_{out}$  is "pulled-up" to the positive supply voltage VDD. In this case the output is the complement of the input. If  $V_{in}$  is greater than  $V_{th}$ , the transistor is switched on and current flows from the VDD supply through the load resistor R to GND. If R were sufficiently large,  $V_{out}$  could be "pulled-down" well below  $V_{th}$ , thus again complementing the input. However, the resistance per unit length of minimum width lines of various available conducting elements is far less than the effective resistance of the switched on MOSFET. Implementing a sufficiently large inverter load using resistive lines would require a very large area compared to that occupied by the transistor itself.

To circumvent this problem a depletion mode MOSFET is used as a pullup for the basic inverter circuit, symbolized and configured as shown in figure 2b. In contrast to the usual

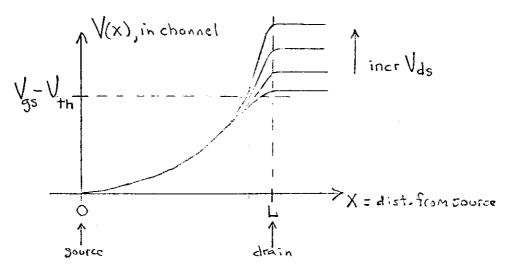


Fig. 1e. VOLTAGE PROFILE ACROSS CHANNEL

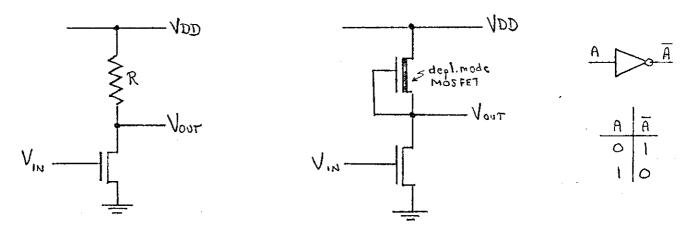


Fig. 2a. AN INVERTER

Fig 2 b. THE BASIC INVERTER,
CIRCUIT PIAGRAM, LOGIC SYMBOL, LOGIC FUNCTION

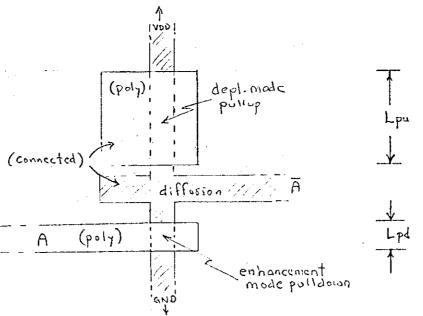


Fig & c. BASIC INVERTER LAYOUT

enhancement mode transistor, the depletion mode transistor has a threshold voltage,  $V_{dep}$ , that is less than zero. During fabrication, one of the masks is used to select any desired subset of transistors in the integrated system for processing as depletion mode transistors. For a depletion mode transistor to turn off, it requires a voltage on its gate relative to its source that is more negative than  $V_{dep}$ . But in this configuration its gate is connected to its source, and thus it is always turned on. Hence, when the enhancement mode transistor is turned off, for example by connecting zero voltage to its gate, the output of the inverter will be equal to VDD. We will find that for reasonable ratios of the gate geometries of the two transistors, input voltages above a defined logic threshold voltage,  $V_{inv}$ , will produce output voltages below that logic threshold voltage.

The top view of the layout of an inverter on the silicon surface is sketched in figure 2c. It consists of two polysilicon regions overhanging a path in the diffusion level which runs between VDD and GND. This arrangement forms the two MOS transistors of the inverter. The inverter input A is connected to the poly forming the gate of the lower of the two transistors. The pullup is formed by connecting the gate of the upper transistor to its source. The fabrication details of such connections will be described in a later chapter. The output of the inverter is shown leaving, on the diffusion level, from between the drain of the pulldown and the source of the pullup. The pullup is a depletion mode transistor, and it is usually several times longer than the pulldown, to insure proper inverter transfer characteristics.

Figures 3a and 3b show the  $I_{ds}$  versus  $V_{ds}$  and  $V_{gs}$  characteristics of a typical pair of MOS transistors used to implement an inverter. The characteristics of the pullup and pulldown differ only in their thresholds and, therefore, in the relative locations of their saturation regions.

We can now use a graphical construct to determine the actual transfer characteristic,  $V_{out}$  vs  $V_{in}$ , of the inverter circuit. From figures 2a and 2b we see that the  $V_{ds}(enh)$  of the enhancement mode transistor equals VDD minus  $V_{ds}(dep)$  of the depletion mode transistor. Also,  $V_{ds}(enh)$  equals  $V_{out}$ . In a steady state and with no current drawn from the output, the  $I_{ds}$  of the two transistors are equal. Since the pullup has its gate connected to its source, only one of its characteristic curves is relevant, namely the one for  $V_{gs}(dep) = 0$ . Taking these facts into account, we begin the graphical solution by superimposing plots of  $I_{ds}(enh)$  vs  $V_{ds}(enh)$ , and the one plot of  $I_{ds}(dep)$  vs  $[VDD - V_{ds}(dep)]$ . Since the currents in both transistors must be equal, the intersections of these sets of curves yields  $V_{ds}(enh) = V_{out}$ 

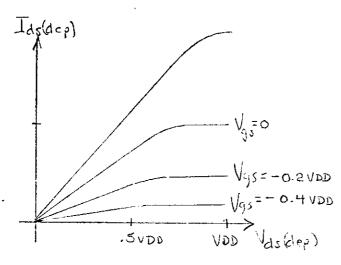
versus  $V_{gs}(enh) = V_{in}$ . The resulting transfer characteristic is plotted in figure 3d.

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Studying figures 3c and 3d, consider the effect of starting with  $V_{in}$  = 0 and then gradually increasing V<sub>in</sub> towards VDD. While the input voltage is below the threshold of the pulldown transistor, no current flows in that transistor, the output voltage is constant at VDD, and the drain to source voltage across the pullup transistor is equal to zero. When Vin is first increased above the enhancement mode threshold, current begins to flow in the pulldown transistor. The output voltage slightly decreases as the input voltage is first increased above V<sub>th</sub>. Subsequent increases in the input voltage rapidly lower the pulldown's drain to source voltage, until the point is reached where the pulldown leaves the saturation region. Then as V<sub>in</sub> continues to increase, the output voltage asymptotically approaches zero. Figure 3d also shows the effect of changes in the transistor length to width ratios on the transfer characteristics and on the logic threshold voltage. The resistive impedance of the MOS transistor is proportional to the length to width ratio Z of its gate region. Using the subscript pu for the pullup transistor and pd for the pulldown transistor: If  $Z_{pu}$  =  $L_{pu}/W_{pu}$  is increased relative to  $Z_{pd} = L_{pd}/W_{pd}$ , then  $V_{inv}$  decreases, and vice-versa. The gain, or negative slope of the transfer characteristic near  $V_{inv}$ , increases as  $Z_{pu}/Z_{pd}$ increases. The gain G must be substantially greater than one for digital circuits to function properly.

## Inverter Logic Threshold Voltage

The most fundamental property of the basic inverter circuit is its logic threshold voltage,  $V_{inv}$ . The logic threshold here is *not* the same as  $V_{th}$  of the enhancement mode transistor, but is that voltage on the input of the enhancement mode transistor which causes an equal output voltage. If  $V_{in}$  is increased above this logic threshold,  $V_{out}$  falls below it, and if  $V_{in}$  is decreased below  $V_{inv}$ ,  $V_{out}$  rises above it. The following simple analysis assumes that both pullup and pulldown are in saturation, so that equation 3 applies. Usually the pullup is not quite in saturation, but the following is still nearly correct.  $V_{inv}$  is approximately that input voltage which would cause saturation current through the pullup which the pullup transistor. Referring to eq.3, we find the condition for equality of the two currents given in eq.4.



Jas=0.5 vap

1/35=0.4 vap

1/35=0.3 vap

Vas=0.3 vap

Vas(enh)

Fig3a. Inverter Pullup Characteristics

Fig 3b. Pulldown Characteristics

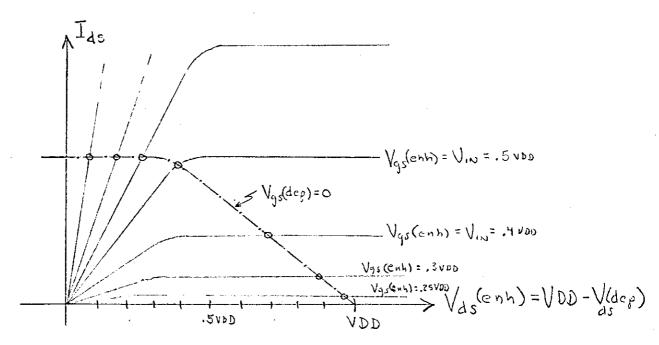


Fig &c. Ids(enh) us Vas(enh) & Ids (dep) vs [VDD - Vas (dep)]

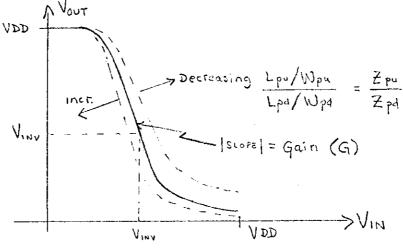


Fig. 3d BASIC INVERTER VOIT US VIN

$$\frac{\text{Wpd}}{\text{Lpd}}(V_{\text{inv}} - V_{\text{th}})^2 = \frac{\text{Wpu}}{\text{Lpu}}(-V_{\text{dep}})^2, \qquad [eq.4]$$

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or thus when:

$$V_{inv} = V_{th} - V_{dep}/[Zpu/Zpd]^{\frac{1}{2}}$$
 [eq.4a]

Here we note that the current through the depletion mode transistor is dependant only on its geometry and threshold voltage  $V_{dep}$ , since its  $V_{gs} = 0$ . Note that  $V_{inv}$  is dependent upon the thresholds of both the enhancement and depletion mode transistors, and also the square root of the ratio of the Z = L/W of the enhancement mode transistor to that of the depletion mode transistor.

Tradeoffs are possible between these system threshold voltages and the areas and current driving capability of transistors in the system's inverters. To maximize  $(V_{gs} - V_{th})$  and increase the pulldowns' current driving capability for a given area,  $V_{th}$  should be as low as possible. However, if  $V_{th}$  is too low, inverter outputs won't be driveable below  $V_{th}$ , and inverters won't be able to turn off transistors used as simple switches. The original choice of  $V_{th} \sim 0.2 \text{VDD}$  is a reasonable compromise here.

Similarly, to maximize the current driving capability of pullups of given area, we might set the system's  $V_{dep}$  as far negative as possible. However, eq. 4a shows that for chosen  $V_{inv}$  and  $V_{th}$ , decreasing  $V_{dep}$  requires an increase in  $L_{pu}/W_{pu}$ , typically leading to an increase in pullup area. The compromise made in this case is usually as follows. The negative threshold of depletion mode transistors is set during fabrication such that with gate tied to source, they turn on approximately as strongly as would an enhancement mode transistor with VDD connected to its gate and its source grounded. In other words, depletion mode and enhancement mode transistors of equal gate dimensions would have equal drain to source currents under those conditions. Applying eq.3 in those conditions we find that:

$$(-V_{dep})^2 \sim (VDD - V_{th})^2$$

Therefore,  $-V_{\rm dep} \sim ({\rm VDD} - V_{\rm th})$ , and  $V_{\rm dep} \sim -0.8 {\rm VDD}$ . While adjustments in the details of this choice are often made in the interest of optimization of processes for a particular product, we will assume here this approximate equality of turn-on voltages of the two transistor types for the sake of simplicity. Substituting this choice of  $V_{\rm dep}$  into eq.4a,

we find that for V<sub>th</sub> small compared to VDD:

$$V_{inv} \sim VDD/[Zpu/Zpd]^{\frac{1}{2}}$$
 [eq.4b]

In general it is desirable that the margins around the inverter threshold be approximately equal, i.e., that the inverter threshold,  $V_{inv}$ , lie approximately midway between VDD and ground. We see from eq.4b that this criterion is met by a ratio of pullup Z to pulldown Z of approximately 4:1. We will see later that the choice of  $V_{dep} \sim VDD - V_{th}$ , producing a ratio of 4:1 here, will lead to a balancing of performances in certain other important circuits.

## Inverter Delay

A minimum requirement for an inverter is that it drive another identical to itself. Let us analyze the delay through a string of inverters of identical dimensions since this is the simplest case in which we can estimate the performance. Assume that the ratio of Z of the pullups to Z of the pulldowns equals k. Inverters connected in this way are shown in Fig. 4a. We will sometimes use the alternative pullup symbol shown ("resistor with gate"), to clarify its functional purpose.

Let us assume that prior to t = 0, the voltage at the input of the first inverter is zero, and hence, the voltage output of the second inverter will be low. At time t=0, let us place a voltage equal to VDD on the input of the first inverter and follow the sequence of events which follows. The output of the first inverter, which leads to the gate of the second inverter, will initially be at VDD. Within approximately one transit time, the pulldown transistor of the first inverter will remove from this node an amount of charge equal to VDD times the gate capacitance of the pulldown of the second inverter. The pullup transistor of the second inverter is now faced with the task of supplying a similar charge to the gate of the third inverter, to raise it to VDD. Since it can supply at most only 1/k'th of the current that can be supplied by the pulldown transistor, the delay in the second inverter stage is approximately k times that of the first.

It is thus convenient to speak of the inverter pair delay which includes the delay for one lowgoing transition and one highgoing transition. This inverter pair delay is approximately (1+k) times the transit time, as shown in figure 4. The fact that the rising transition is

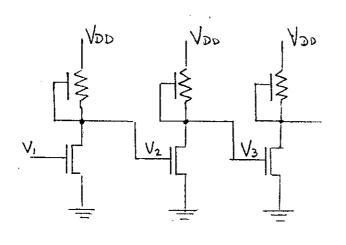
slower than the falling transition by approximately the inverter transistors' geometry ratios is an inherent characteristic of any ratio type logic. It is not true of all logic families. For example, in families such as complementary MOS where there are both pMOS and nMOS devices on the same silicon chip and both types operate strictly as pulldown enhancement mode devices, any delay asymmetry is a function of the difference in mobilities of the p and n type charge carriers rather than of the transistor geometrical ratios.

Fig. 4b shows an inverter driving the inputs of several other inverters. In this case, for a fanout factor f, it is clear that in either the pullup or pulldown direction, the active device must supply f times as much charge as it did in the case of driving a single input. In this case, the delay both in the up and downgoing directions is increased by approximately the factor f. In the case of the downgoing transition, the delay is approximately f times the transit time of the pulldown transistor, and in the case of the upgoing transition, the delay is approximately the inverter ratio k times the fanout factor times the pulldown transit time.

In the discussions of transit time given earlier, it was assumed that both the depletion mode pullup device and the enhancement mode pulldown device were operating in the saturation region where they act like current sources. It was also assumed that all capacitances were constant, and not a function of voltage. This condition is not strictly met in the technology we are discussing. Delay calculations given in this text are based on a "switching model" where individual stages spend a small fraction of their time in the mid-range of voltages around  $V_{\rm inv}$ . This assumption introduces a small error of the order of 1/G. Because of these and other second order effects, the switching times actually observed vary somewhat from those derived.

## Parasitic Effects

In integrated systems, capacitances of circuit nodes are due not only to the capacitance of gates connected to the nodes, but also include capacitances to ground of signal paths connected to the nodes and other stray capacitances. These other capacitances, sometimes called parasitic or stray capacitances, are not negligible. While gate capacitances are typically an order of magnitude greater per unit area than the capacitances of the signal paths, the signal paths may sometimes be larger in area than the associated gate regions. Therefore, a substantial fraction of the delay encountered may be accounted for by stray capacitance rather than by the inherent properties of the active transistors. In the simplest



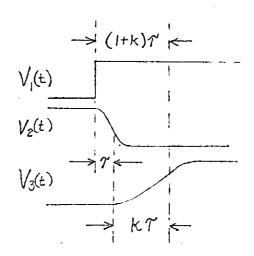
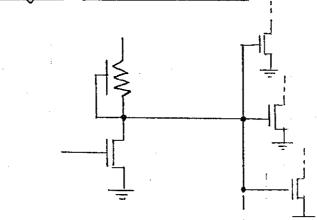
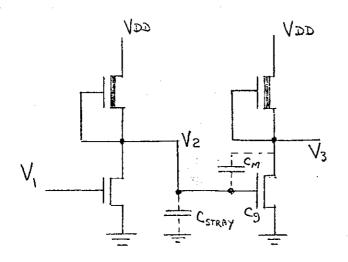


Fig. 4a. INVERTER DELAY



for fanout of f: down delay ~ fr up delay ~ kfr

Fig.46. FANOUT



START: Vz=0, V3=1 Qg=0, Qm=-Cm

FINISH: V2=1, V3=0
Q5=C9, QM=+CM

Fig. 5. MILLER EFFECT

Tot. Effect. Input Cap = Cg + 2Cm + Cstray

case where the capacitance of a node is increased by the presence of parasitic area attached to the node, the delays can be accounted for by simply increasing the transit time by the ratio of the total capacitance to that of the gate of the transistor being driven. We now require time to supply charge not only to the gate itself but also to the parasitic capacitance.

There is one type of parasitic, however, which is not accounted for so simply. All MOS transistors have a parasitic capacitance between the drain edge of the gate and the drain node. This effect is shown schematically in figure 5. In an inverter string such as that mentioned earlier, this capacitance will be charged in one direction for one polarity of input, and in the opposite direction for the opposite polarity input. Thus, on a gross scale its effect on the system is twice that of an equivalent parasitic capacitance to ground. Therefore, gate to drain capacitances should be approximately doubled, and added to the gate capacitance  $C_g$  and the stray capacitances, to account for the total capacitance of the node and thus for the effective delay time of the inverter. The effective inverter pair delay then =  $\tau(1+k)C_{total}/C_g$ .

## Driving Large Capacitive Loads

As we have seen, the delay per inverter stage is multiplied by a fanout factor. The overall performance of a system may be seriously degraded if it contains any large fanouts, where one circuit within the system is required to drive a large number of circuits similar to itself. As we shall see, this situation often occurs in the case of control drivers which are required to drive a large number of inputs to memory cells or logic function blocks. A similar and even more serious problem is driving wires which go off the silicon chip to other chips or input/output devices. In such cases the ratio of the capacitance which must be driven to the inherent capacitance of a gate circuit on the chip is often many orders of magnitude, causing a serious delay and a degradation of system performance.

Consider how we may drive a capacitive load  $C_L$  in the minimum possible time given that we are starting with a signal on the gate of an MOS transistor of capacitance  $C_g$ . Define the ratio of the load capacitance to the gate capacitance,  $C_L/C_g$ , as Y. It seems intuitively clear that the optimum way to drive a large capacitance is to use our elementary inverter to drive a larger inverter and that larger inverter to drive a still larger inverter until at some point the larger inverter is able to drive the load capacitance directly. Using an argument similar to the fanout argument it is clear that for one inverter to drive another inverter, where the

second is larger in size by a factor of f, results in a delay f times the inherent inverter delay,  $\tau$ . If n such stages are used, each larger than the previous by a factor f, then the total delay of the inverter chain is  $nf\tau$ , where  $f^n$  equals Y. Note that if we use a large factor f, we can get by with few stages, but each stage will have a long delay. If we use a smaller factor f, we can shorten the delay of each stage, but are required to use more stages. What value of n minimizes the overall delay for a given Y? We compute this value as follows:

Delay of one stage 
$$= f\tau = (Y)^{1/n}\tau,$$
Thus total delay is 
$$= F(n) = n(Y)^{1/n}\tau, \text{ and } [eq.5]$$

$$dF(x)/dx = \tau(Y)^{1/x}[1 - \ln Y/x]$$

The function dF(x)/dx equals 0, and thus F(x) is minimum, when  $x = \ln Y$ . Therefore the total delay is minimized when  $n \sim \ln Y$ . Total delay is minimized when each stage is larger than the previous one by a factor of e, the base of natural logarithms. Minimum total delay is the elementary inverter delay  $\tau$  times e times the natural logarithm of the ratio of the load capacitance to the elementary inverter capacitance.

Min. total delay ~ 
$$\tau e[\ln(C_L/C_g)]$$
 [eq.5a]

## Space vs Time

From the results of the sections on inverter delay, parasitic effects, and driving large capacitances, we see that areas and distances on the silicon surface trade off against delay times. For an inverter to drive another inverter some distance away, it must charge not only the gate capacitance of the succeeding inverter but also the capacitance to ground of the signal path connecting the two. Increasing the distance between the two inverters will therefore increase the inverter pair delay. This effect can be counterbalanced by increasing the area of the first inverter, so as to reduce the ratio of the load capacitance to the gate capacitance of the first inverter. But the delay of some previous driving stage is then increased. There is no way to get around the fact that transporting a signal from one node to another some distance away requires charging or discharging capacitance, and therefore

takes time. Note that this is not a velocity of light limitation as is often the case outside the chip. The times are typically several orders of magnitude longer than those required for light to traverse the distances involved. To minimize both the time and space required to implement system functions, we will tend to use the smallest possible circuits and locate them in ways which tend to minimize the interconnection distances.

The results of a previous section can be used here to illustrate another interesting space vs time effect. Suppose that the minimum size transistors of an integrated system have a transit time  $\tau$  and gate capacitance  $C_g$ . A minimum size transistor within the system produces a signal which is then passed through successively larger inverting logic stages and eventually drives a large capacitance  $C_L$  with minimum total delay equal to  $t_{min}$ . With the passage of time, fabrication technology improves and we replace the system with one in which the circuits are all scaled down in size by dividing by a factor  $\alpha$  (the motivation for this is clear: the new system may contain  $\alpha^2$  as many circuits). As described in a later section, we will find that the transit times of the smallest circuits will now be  $\tau' = \tau/\alpha$ , and their gate capacitance will be  $C_g' = C_g/\alpha$ . Referring to equation 5a., we find that the new minimum total delay,  $t_{min}'$ , to drive  $C_L$  is:

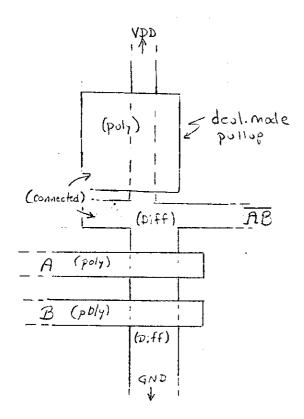
$$t_{\min}' = t_{\min}[(1/\alpha)\ln(\alpha)]$$

Therefore, as the inverters scale down and  $\tau$  gets smaller, more inverting logic stages are required to obtain the minimum offchip delay. Thus the relative delay to the outside world becomes larger. However, the absolute delay becomes smaller.

## Basic NAND and NOR Logic Circuits

NAND and NOR logic circuits may be constructed in integrated systems as simple expansions of the basic inverter circuit. The analysis of the behavior of these circuits, including their logic threshold voltages, transistor geometry ratios and time delays, is also a direct extension of the analysis of the basic inverter.

The circuit layout diagram of a two input NAND gate is shown in figure 6a. The layout is that of a basic inverter with an additional enhancement mode transistor in series with the pulldown transistor. NAND gates with more inputs may be constructed by simply adding more transistors in series with the pulldown path. The electrical circuit diagram, truth table



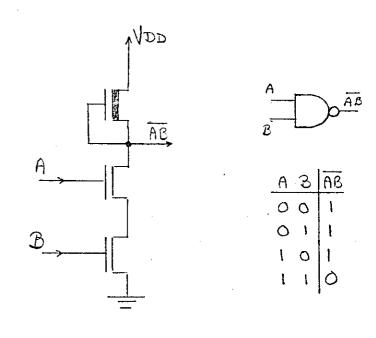


Fig. Ga. NAND GATE (top view)

Fig. 6 b. NAND GATE, CIRCUIT DIAGRAM, LOGIC SYMBOL, LOGIC FUNCTION

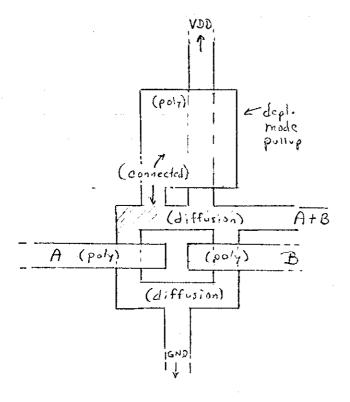


Fig. Ge. NOR GATE (Top View)

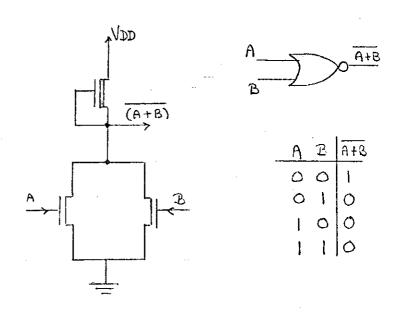


Fig G.d NOR GATE, CIRCUIT DAGRAM LOGIC STANGOL, LOGIC FUNCTION

and logic symbol for the two input NAND gate are shown in figure 6b. If either of the inputs A or B is a logic-0, the pulldown path is open and the output will be high, and therefore a logic-1. For the output to be driven low, to logic-0, both inputs must be high, at logic-1. The logic threshold voltage of this NAND gate is calculated in a similar manner to that of the basic inverter, except equation 4b is rewritten with the length of the pulldowns replaced with the sum of the lengths of the two pulldowns (assuming their widths are equal) as follows:

$$V_{thNAND} \sim VDD/[(Lpu/Wpu)/((Lpd_a+Lpd_b)/Wpd)]^{1/2}$$

This equation indicates that as pulldowns are added in series to form NAND gate inputs, the pullup length must be enlarged to hold the logic threshold voltage constant. The logic threshold voltage of an n-input NAND gate, assuming all the pulldowns have equal geometries, is:

$$V_{thNAND} \sim VDD/[(Lpu/Wpu)/(nLpd/Wpd)]^{\frac{1}{2}}$$

As inputs are added and pullup length is increased, the delay time of the NAND gate is also correspondingly increased, both for rising and falling transitions.

$$\tau_{NAND} \sim n\tau_{inv}$$

The circuit layout diagram of a two input NOR gate is shown in figure 6c. The layout is that of a basic inverter with an additional enhancement mode transistor in parallel with the pulldown transistor. Additional inputs may be constructed by simply placing more transistors in parallel with the pulldown path. The circuit diagram, truth table and logic symbol for the two input NOR gate are shown in figure 6d. If either of the inputs A or B is a logic-1, the pulldown path to ground is closed and the output will be low, and therefore a logic-0. For the output to be driven high, to logic-1, both inputs must be low, at logic-0. If one of its inputs is kept at logic-0, and the other swings between logic-0 and logic-1, the logic threshold voltage of the this NOR gate is the same as that of a basic inverter of equal pullup to pulldown ratio. If this ratio were 4:1 to provide equal margins, then  $V_{\rm thNOR} \sim VDD/2$  with only one input active. However, if both pulldowns had equal geometries, and if both inputs were to move together between logic-0 and logic-1,  $V_{\rm thNOR}$  would be reduced to  $\sim VDD/(8)^{\frac{1}{2}}$ . The logic threshold voltage of an n-input NOR circuit decreases as a function of the number of active inputs (inputs moving together from logic-0 to logic-1).

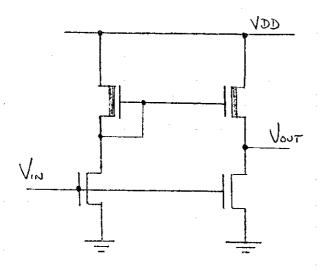
The delay time of the NOR gate with one input active is the same as that of an inverter of equal transistor geometries, except for added stray capacitance. Its delay time for falling transitions is decreased as more of its inputs are active.

### Super Buffers

As we have noted, ratio type logic suffers from an asymmetry in its ability to drive capacitive loads. This asymmetry results from the fact that the pullup transistor has of necessity less driving capability than the pulldown transistor. There are, however, methods for avoiding this asymmetry. Shown in figures 7a and 7b are circuits for inverting and a non-inverting drivers, which are approximately symmetrical in their capability of sourcing or sinking charge into a capacitive load. Drivers of this type are called *super buffers*.

Both types of super buffer are built using a depletion mode pullup transistor and an enhancement mode pulldown transistor, with a ratio of Z's of approximately 4:1 as in the basic inverter. However, the gate of the pullup transistor, rather than being tied to its source, is tied to a signal which is the complement of that driving the pulldown transistor. When the pulldown transistor gate is at a high voltage, the pullup transistor gate will be approximately at ground, and the current through the super buffer will be similar to that through a standard inverter of the same size. However, when the gate of the pulldown transistor is put to zero, the gate of the pullup transistor will go rapidly to 5 volts since it is the only load on the output of the previous inverter, and the depletion mode transistor will be turned on at approximately twice the drive which it would experience if its gate were tied to its source. Since the current from a device in saturation goes approximately as the square of the gate voltage, the current sourcing capability of a super buffer is approximately four times that of a standard inverter. Hence, the current sourcing capability of its pulldowns, and wave forms from super buffers driving capacitive loads are nearly symmetrical.

The effective delay time,  $\tau$ , of super buffers is thus reduced to approximately the same value for highgoing and lowgoing wave forms. Needless to say, when large capacitive loads are to be driven, super buffers are universally used. The arguments used in the last section to determine how many stages are used to drive a large capacitive load from a small source apply directly to super buffers as well.



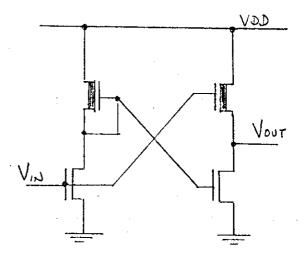


Fig 7a. INVERTING SUPER BUFFER

Fig 7 b. Non-INVERTING SUPER BUFFER

#### A Closer Look at the Electrical Parameters

Up to this point we have talked in very simple terms about the properties of the MOS transistors. They have had a capacitance associated with their gate input and a transit time associated with current flowing from the source to the drain. In the saturation region where the drain to source voltage is high enough, the transistor acts as a current source. The current flowing from drain to source is a function only of the gate to source voltage as given by eq. 3. However, MOS transistors act as current sources only over a fraction of the range encountered in normal operation. Figure 9a summarizes the various regions of MOS transistor operation. Note that once the voltage from drain to source is smaller than the gate voltage minus the threshold voltage, the field in the channel is determined by the drain to source voltage rather than by the gate voltage. As the drain to source voltage decreases below this point, the transit time increases, since the electric field in the channel is lower. For low drain to source voltages, the characteristic of the device is given in eq. 7a.

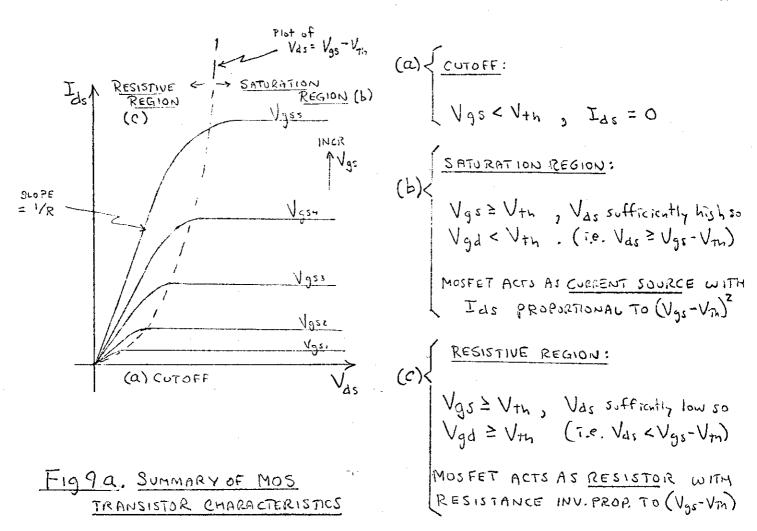
$$I_{ds} = Q/\tau = \mu C_g [(V_{gs} - V_{th}) V_{ds} - (V_{ds}^2)/2]/L^2$$
 [eq.7a]

For very low drain to source voltages, we may neglect the  $V_{ds}^{2}$  term, and the characteristic of the device is given in eq. 7b.

$$I_{ds} = Q/\tau = \mu C_g [(V_{gs} - V_{th}) V_{ds}]/L^2$$
 [eq.7b]

Note that in this region, the drain current is proportional to the source-drain voltage and also to the gate voltage above threshold. The electric field along the channel is uniform at very low  $V_{ds}$ , and hence there is no factor of 2 as there was in equation 3. Any device with a current through it proportional to the voltage across it, may be viewed as a resistor, and in the case of an MOS device with *low* drain to source voltage, the resistance is given by eq. 8. Note, however, that the resistance increases as  $V_{ds}$  increases towards  $V_{gs}$ - $V_{th}$ , as shown by the decreasing slopes of the transfer characteristics in figure 9a as the device nears saturation.

$$V_{ds}/I_{ds} = R = L^2/[\mu C_g(V_{gs} - V_{th})]$$
 [eq.8]



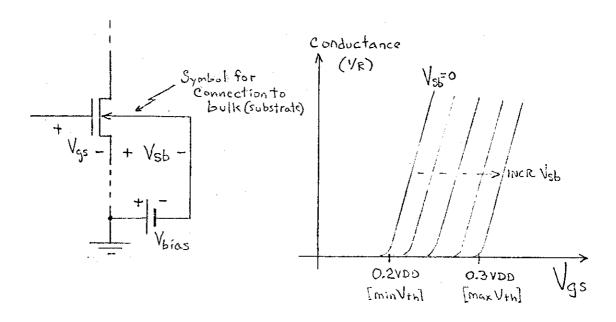


Fig. 96 THE BODY EFFECT

In both equations 7 and 8, the capacitance is the gate to channel capacitance of the turned on transistor. In the simple case where this transistor is driving the gate of another one identical to it, the time response of the system will be an exponential with a time constant RC, given in eq. 9. This time constant is similar to the transit time  $\tau$  given in eq. 1.

$$RC_g = L^2/[\mu(V_{gs} - V_{th})] = \tau/2$$
 [eq.9]

There is another electrical characteristic we may occasionally have to take into account. It turns out that the threshold voltage of an MOS transistor is not a constant, but varies slightly as a function of the voltage between the source terminal of the transistor and the silicon substrate, which is usually ground. This is the so called body effect which is illustrated in figure 9b. If the source to bulk (substrate) voltage,  $V_{sb}$ , equals zero, then  $V_{th}$  is at its minimum value of approximately 0.2 VDD. As  $V_{sb}$  is increased,  $V_{th}$  increases slightly. For typical processes,  $V_{th}$  reaches a maximum value of about 0.3 VDD for  $V_{sb} \sim$  VDD.  $V_{dep}$  is similarly affected, ranging from about -0.8 VDD to -0.7 VDD as the  $V_{sb}$  of a depletion mode MOSFET is raised from zero to VDD volts. As shown in figure 9b, it is possible to insert a fixed bias voltage between the circuit ground and the substrate (rather than just have these be identical). Such a substrate bias provides an electrical mechanism for setting the threshold to an appropriate value.

## Depletion Mode vs Enhancement Mode Pullups

With its gate tied to VDD, a standard enhancement mode transistor would always be on, and thus could be used for a load device in inverting logic circuits. Early MOS processes used pullup devices of exactly this type.

In this section we will make a comparison of the rising transients of the two types of pullup circuits. As noted earlier, rising transients in ratio type logic are usually slower than falling transients, and thus rising transients generally have greater impact on system performance. In the simplest cases, this asymmetry in the transients results from the current sourcing capability of the pullup transistor being less than that of its pulldown counterpart. The simple intuitive time arguments given earlier are quite adequate for making estimates of system performance in most of these cases. However, there are situations in which the

transient time may be much longer than a naive estimate would indicate. The rising transient of the enhancement mode pullup is one of these.

A depletion mode pullup transistor feeding a capacitive load is shown schematically in figure 10a. Since  $V_{gs} \ge V_{th}$  and  $V_{gd} \ge V_{th}$ , the pullup transistor is in the resistive region. The final stages of the rising transient are given by the following exponential:

$$V(t) = VDD[1 - e^{-t/(RC_L)}]$$

For this case of pullup transistor,  $V_{gs}$  is equal to zero, the threshold voltage is a negative  $V_{dep}$ , and the time-constant of the rising transient, derived from eq. 9, is given by eq. 10. Note, by the way, that  $RC_L$  is inversely proportional to  $-V_{dep}$ . As expected, the presence of a larger load capacitance has the effect of simply lengthening the transit time of the circuit by the ratio of the load capacitance to the gate capacitance of the pullup.

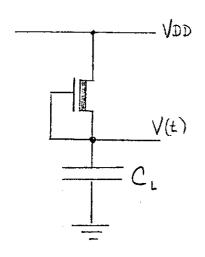
$$RC_L = L^2C_L/\mu C_g \ (-V_{dep}) = \tau \ C_L/2C_g$$
 [eq.10]

A somewhat more complicated situation is presented by an enhancement mode transistor sourcing charge into a capacitive load. This situation is shown schematically in Fig. 10b. Note that since  $V_{gd} = 0$ , the transistor is in saturation whenever  $V_{gs} > V_{th}$ . The problem with sourcing charge from the enhancement mode transistor is that as the voltage at the output node gets closer and closer to one threshold below VDD, the amount of current provided by the enhancement mode transistor goes down rapidly. The current dependence upon the output voltage V is given in eq. 11.

$$Q = -\frac{\varepsilon WL}{D} [(VDD - V_{th}) - V]$$

$$\tau = 2L^2/\mu[(VDD - V_{th}) - V]$$

$$I_{ds} = -Q/\tau = \frac{\mu \epsilon W [(VDD - V_{th}) - V]^2}{2LD}$$
 [eq.11]



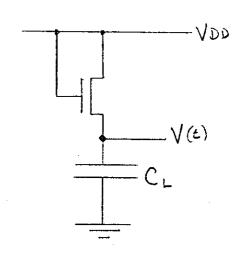


Fig 10a. DEPLETION MODE MOSFET
PULLING UP CAPACITIVE LOAD

Fig 10 b. ENHANCEMENT MODE MOSFET PULLING UP CAPACITIVE LOAD

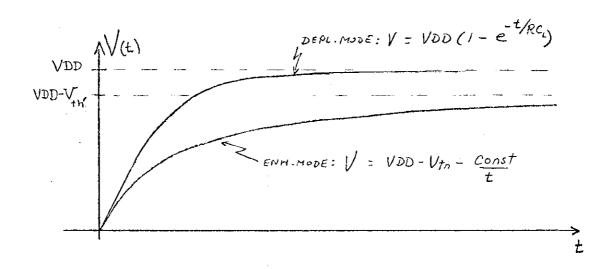


Fig. 10 c. COMPARISON OF RISING TRANSIENTS FOR THE TWO TYPES OF LOADS.

The fact that the pullup current decreases as the output voltage nears its maximum value causes the rising transient from such a circuit to be of qualitatively different form than that of a depletion mode pullup. Equating  $I_{ds} = C_L dV/dt$  with the expression in equation 11, and then solving for V(t), yields the rising voltage transient in equation 12:

$$V(t) = VDD - V_{th'} - C_L \underline{LD}_{\mu \varepsilon Wt}$$
 [eq.12]

Note that in this configuration, the threshold voltage Vth' of the pullup is near its maximum value as V(t) rises towards VDD, due to the body effect. A comparison of the rising transients of the preceding two circuits, assuming the same load capacitance and the same pullup source current at zero output voltage, is shown in Fig. 10c. The rising transient for the depletion mode pullup transistor is crisp and converges rapidly towards VDD. However, the rising transient for the enhancement mode pullup transistor, while starting rapidly, lags far behind and within the expected time response of the system, never even comes close to one threshold below VDD. Even for very large t,  $V(t) < VDD - V_{th'}$ . The practical effect of this property of enhancement mode transistors is that circuits designed to work from a voltage derived from the output of such a circuit should be designed with an inverter threshold  $V_{inv}$  at a considerably lower value than those designed to work with the output of a depletion mode pullup circuit. In order to obtain equal inverter margins without sacrificing performance, we will normally use depletion mode pullups.

## Delays in Another Form of Logic Circuitry

Enhancement mode transistors, when used in small numbers and driving small capacitive loads, may often be used as switches in circuits of simple topology to provide logic signal steering functions of much greater complexity than could be easily achieved in ratio type inverting logic. These circuits are reminiscent of relay switching logic, and transistors used in this way are referred to as "pass transistors" or "transmission gates". Example circuits using this type of design are given in Chapter 3. A particularly interesting example is the Manchester carry chain<sup>5</sup>, used for propagating carry signals in parallel adders. In each stage of the adder a carry propagate signal is derived from the two input variables to the adder, and if it is desired to propagate the carry, this propagate signal is applied to the gate of an

4

enhancement mode pass transistor. The source of the transistor is carry-in to the present stage, and the drain of the transistor is carry-out to the next stage. In this way, a carry can be propagated from less to more significant stages of the adder without inserting a full inverter delay between stages. The circuit is shown schematically in Fig. 11a.

The delay through such a circuit does not involve inverter delays but is of an entirely different sort. A voltage along the chain divides into  $V_{\rm ds}$  across each pass transistor. Thus  $V_{\rm ds}$  is usually low, and the pass transistors operate primarily in the resistive region. We can think of each transistor as a series resistance in the carry path, and a capacitance to ground formed by the gate to channel capacitance of each transistor, and the strays associated with the source, drain, and connections with the following stage. An abstraction of the electrical representation is shown in Fig. 11b. The minimum value of R is the turned on resistance of each enhancement mode pass transistor, while the minimum value of C is the capacitance from gate to channel of the pass transistor. Strays will increase both values, in particular that of C. The response at the node labelled  $V_2$  with respect to time is given in eq. 13. In the limit as the number of sections in the network becomes large, eq. 13 reduces to the differential form shown in eq. 14 where R and C are now the resistance and capacitance per unit length, respectively.

$$C dV_2/dt = [(V_1 - V_2) - (V_2 - V_3]/R$$
 [eq.13]

$$RC dV/dt = d^2V/dx^2$$
 [eq.14]

Equation 14 is the well-known diffusion equation, and while its solutions are complex, in general the time required for a transient to propagate a distance x in such a system is proportional to  $x^2$ . One can see qualitatively that this might be so. Doubling the number of sections in such a network doubles both the resistance and the capacitance, and therefore causes the time required for the system to respond to increase by a factor of approximately four. The response of a system of n stages to a step function input is shown in Fig. 11c.

If we add one more pass transistor to such a chain of n pass transistors, the added delay through the chain is small for small n, but very large for large n. Therefore, it is highly desirable to group the pass transistors used for steering, multiplexing, and carry-chain type logic into short sections and interpose inverting logic between these sections. This approach applied to the carry chain is shown in figure 11d. The delay through a section of n pass

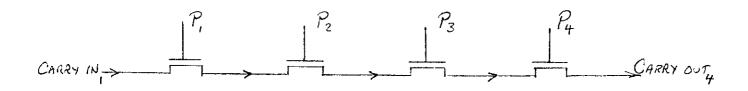


Fig. 11a. PASS TRANSISTOR CHAIN PROPOGATING A CARRY SIGNAL

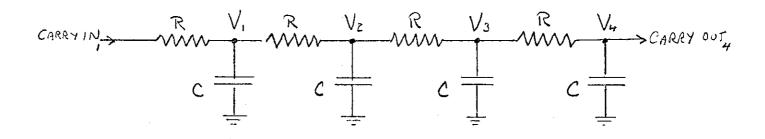


Fig 116. EQUIVALENT CIRCUIT

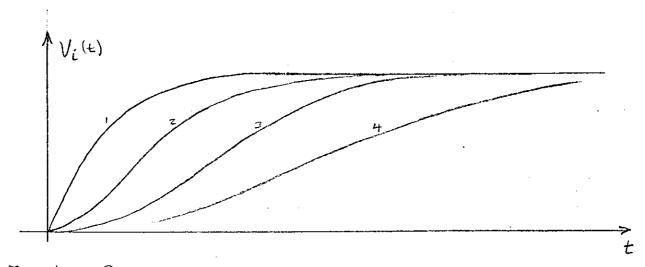


Fig. 11c. RESPONSE TO STEP FUNCTION INPUT

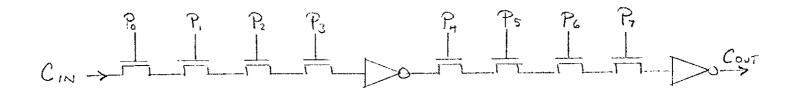


Fig 11d. MINIMIZHE DELAY BY INTERPOSING INVERTERS

transistors is proportional to  $RCn^2$ . Thus the total delay is  $kRCn^2$  plus the delay through the inverter  $\tau_{inv}$ . The average delay per stage is given in eq. 15. To minimize the delay per stage, n should be chosen such that the delay through the n pass transistors is just equal to the inverter delay.

Total delay = 
$$kRCn^2 + \tau_{inv}$$
,

Average delay/stage =  $kRCn + \tau_{inv}/n$  [eq.15]

Min. delay when:  $kRCn^2 = \tau_{inv}$ 

Since logic done by steering signals with pass transistors does not require static power dissipation, a generalization of this result may be formulated. It pays to put as much logic into steering type circuits as possible until there are enough pass transistors to delay the signal by approximately one inverting logic delay. At this point, the level of the signal can be restored by an inverting logic stage and the processing proceed from there.

The pass transistor has another important advantage over an inverting logic stage. When used to control or steer a logic signal, the pass transistor has only an input, control, and output connections. A NAND or NOR logic gate implementing the same function, in addition to containing two more transistors and thus occupying more area, also requires VDD and GND connections. As a result, the topology of interconnection of pass transistor circuits is far simpler than that of inverting logic circuits. This topological simplicity of pass transistor control gates is an important factor in the system design concepts developed in later chapters.

## Pullup/Pulldown Ratios for Inverting Logic Coupled by Pass Transistors

Early in this chapter we found that when an inverting logic stage directly drives another such stage, a pullup to pulldown ratio  $Z_{pu}/Z_{pd} = (L_{pu}/W_{pu})/(L_{pd}/W_{pd})$  of 4:1 yields equal inverter margins and also provides an output sufficiently less than  $V_{th}$  for an input equal to VDD. Rather than coupling inverting logic stages directly, we often couple them with pass transistors for the reasons developed in the preceding section, thus affecting the required pullup to pulldown ratio.

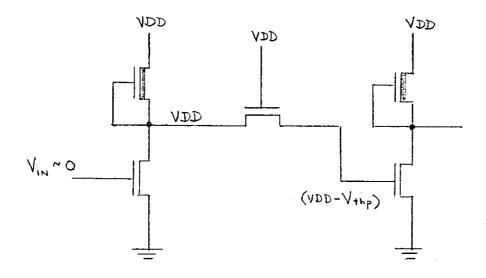


Figure 12a. Inverters Coupled by Pass Transistor

$$\frac{Z_{pu}}{Z_{pd}} = \frac{L_{pv}/W_{pv}}{L_{pd}/W_{pv}} = \frac{L_{pv}/W_{pv}}{L_{pd}/W_{pv}}$$

$$VDD \longrightarrow R_{1}$$

$$(VDD - V_{thp}) \longrightarrow R_{2}$$

Figure 12b. FOT VOUTZ = VOUTI, Zpuz/Zpdz = 8.

Figure 12a shows two inverters connected by a pass transistor. If the output of the first inverter nears VDD, the input of the second inverter can at most rise to  $(VDD - V_{thp})$ , where  $V_{thp}$  is the threshold of the pass transistor. Even with VDD on its gate, the pass transistor opens the connecting path once its input side rises above  $(VDD - V_{thp})$ . For the second inverter to have its output driven as low with an input of  $(VDD - V_{thp})$  as would a standard inverter with an input of VDD, it must have a larger pullup to pulldown ratio, calculated as follows.

With inputs near VDD, the pullups of inverters are in saturation, and the pulldowns are in the resistive region. Figure 12b shows equivalent circuits for two inverters, one with VDD as input, the other with (VDD -  $V_{thp}$ ). For their output voltages to be equal under these conditions,  $I_1R_1$  must equal  $I_2R_2$ , and substituting from eq.3 and eq.8 we find:

$$(Z_{pu1}/Z_{pd1})(VDD - V_{th}) = (Z_{pu2}/Z_{pd2})(VDD - V_{th} - V_{thp})$$

Since  $V_{th}$  of the pulldowns ~ 0.2VDD, and  $V_{thp}$  of the pass transistor ~ 0.3VDD due to the body effect, then  $Z_{pu2}/Z_{pd2} \sim 2Z_{pu1}/Z_{pd1}$ . Thus a ratio  $(L_{pu}/W_{pu})/(L_{pd}/W_{pd}) = 8$  is usually used for inverting logic stages placed as level restorers between sections of pass transistor logic.

#### Properties of Cross-Coupled Circuits

In many control sequencing and data storage applications, memory cells and registers are built using two inverters driving each other, as shown in figure 13a. This circuit can be set in either the state where  $V_1$  is high and  $V_2$  is low, or in the state where  $V_2$  is low and  $V_1$  is high. In either case, the condition is stable and will not change to the other condition unless it is forced there through some external means. The detailed methods of setting such cross-coupled circuits into one state or another will be discussed in detail later. However, it is important at the present time to understand the time evolution of signals impressed upon cross-coupled circuits, since they exhibit properties different from circuits not having a feedback path from their output to an input.

We have seen that there exists a voltage at which the output of an inverter is approximately equal to its input voltage. If a cross-coupled circuit is inadvertently placed in a situation where its input voltage is equal to this value, then an unstable equilibrium condition is

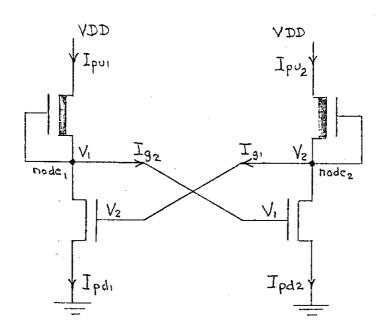


Fig 13a. CROSS COUPLED INVERTERS

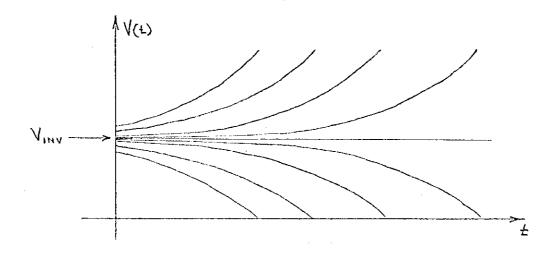


Fig 13b. V(t) FOR CROSS COUPLED INVERTERS

created where voltages  $V_1$  and  $V_2$  are equal. Since the net current flowing onto either gate is now zero, there is no forcing function driving the system to any voltage other than this equilibrium one, and the circuit can stay in this condition for an indefinite period. However, if either voltage changes, even very slightly, the circuit will leave this unstable equilibrium. For example, if the voltage  $V_1$  is increased from its unstable equilibrium value  $V_{inv}$  by a slight amount, this will in time cause a lowering of voltage  $V_2$ , as net current flows from gate 1. This lowering of  $V_2$  will at some later time cause  $V_1$  to increase further. As time goes on, the circuit will feedback on itself until it rests in a stable equilibrium state.

The possibility of such unstable equilibria in cross coupled circuits has important system implications<sup>2</sup>, as we will later see. For this reason, we will make a fairly detailed analysis of this circuit's behavior near the metastable state. While it is not essential that the reader follow all the details of the analysis, the final result should be carefully studied. The time constant of the final result depends in detail on the regions of operation of the transistors near the metastable state, as given in the following analysis. However, the exponential form of the result follows simply from the fact that the forcing function pushing the voltage away from the metastable point is proportional to the voltage's distance away from that point. This behavior is characteristic of bistable storage elements in any technology.

The time evolution of this process can be traced as follows. At the unstable equilibrium, the current in the pullups equals that in the pulldowns, and is a constant times  $(V_{inv}-V_{th})^2$ . If  $V_1$  is then changed by some small  $\Delta V_1$  to  $V_{init}$ ,  $I_{pu2}$  remains constant but  $I_{pd2}$  changes immediately, producing a non-zero  $I_{g1}$ :

$$I_{g1} = I_{pu2} - I_{pd2} = k[(V_{inv} - V_{th})^2 - (V_{inv} + \Delta V_1 - V_{th}^2)]$$

For small  $\Delta V_1$ ,  $I_{g1} = -2k(V_{inv} - V_{th})\Delta V_1$ . More precisely, since  $I_{g1} = function(V_1, V_2)$ , then near  $V_{inv}$ :

$$\partial l_{g1}/\partial V_1 = -2k(V_{inv}-V_{th})$$

Noting that the pullups are not quite in saturation, but are in the resistive region, and:

$$\partial I_{g1}/\partial V_2 = -1/R_{pu}$$
,

where  $R_{pu}$  = effective resistance of the pullup near  $V_{inv}$ . Noting that  $I_{g1} = C_g dV_{g2}/dt$ , we find that:

$$dI_{g1}/dt = -2k(V_{inv}-V_{th})[dV_{1}/dt] - (1/R_{pu})[dV_{2}/dt] = C_{g}[d^{2}V_{2}/dt^{2}]$$

Evaluating the constants in this equation yields  $-2k(V_{inv}-V_{th}) = C_g/\tau_o$ , where  $\tau_o$  is the transit time of the pulldowns for t near zero. Evaluating the effective resistance of the pullups in terms of the parameters of the pulldowns yields  $1/R_{pu} \sim C_g/\tau_o$ . Therefore:

$$-(2/\tau_o)[dV_1/dt] - (1/\tau_o)[dV_2/dt] = d^2V_2/dt^2$$
 Similarly: 
$$-(2/\tau_o)[dV_2/dt] - (1/\tau_o)[dV_1/dt] = d^2V_1/dt^2$$

Near t = 0,  $dV_1/dt$  approximately equals  $- dV_2/dt$ , and therefore:

$$d^2V_1/dt^2 = -(1/\tau_0) dV_2/dt = (1/\tau_0)^2 V_1 + const.$$
 [eq.16a]

The solution to eq. 16a is an exponential diverging from the equilibrium voltage  $V_{inv}$  with time, with a time constant  $\tau_0/2$  equal to one half the pulldown delay time. Note that the solution given in eq.16b satisfies the conditions that  $V(0) = V_{init}$ , and V(t) = constant if  $V_{init} = V_{inv}$ :

$$V_1(t) = V_{inv} + (V_{init} - V_{inv}) e^{t/\tau_0}$$
 [eq.16b]

If a circuit has truly been balanced at the equilibrium voltage, it will only be able to move from this value by virtue of noise or external stimuli. However, in real systems such stimuli are always present and the length of time which it will take for the inverter to settle into one of its stable states is dependent upon how far the initial voltage is from the unstable equilibrium. Various models have been made of this process, making certain assumptions about the statistics of the stimuli tending to unbalance the balanced device. The details of these models are unimportant. What is important for the present purpose is that it is possible to balance any cross-coupled memory device in such a way that the time required for it to recover is arbitrarily long. The time evolution of such a system is shown in Fig. 13b, for several initial voltages near  $V_{\rm inv}$ . The time for the cross-coupled system to reach one of its equilibria is thus logarithmic in the displacement from  $V_{\rm inv}$ , and is given approximately by eq. 16c:

$$t \sim \tau_0 \ln[V_{inv}/(V_{init}-V_{inv})]$$
 [eq.16c]

# Effects of Scaling Down the Dimensions of MOS Circuits and Systems

This section examines the effects on important system parameters resulting from scaling down all dimensions of an integrated system, including those vertical to the surface, by dividing them by a constant factor  $\alpha$ . The voltage is likewise scaled down by dividing by the same constant factor  $\alpha$ . Using this convention, all electric fields in the circuit will remain constant and hence many non-linear factors affecting performance will not change as they would if a more complex scaling were used.

Figure 14a. shows a MOSFET of dimensions L, W, D, with a (Vgs - Vth) = V. Figure 14b. shows a MOSFET similar to that in figure 14a., but of dimensions L' =  $L/\alpha$ , W' =  $W/\alpha$ , D' =  $D/\alpha$ , and V' =  $V/\alpha$ . Refer to equations 1., 2., and 3. From these equations we will find that as the scale down factor  $\alpha$  is increased, the transit time, the gate capacitance, and drain to source current of every individual transistor in the system scale down proportionally, as follows:

$$\tau \propto L^2/V, \quad \tau'/\tau = [(L/\alpha)^2/(V/\alpha)]/[L^2/V], \quad \therefore \quad \tau' = \tau/\alpha$$

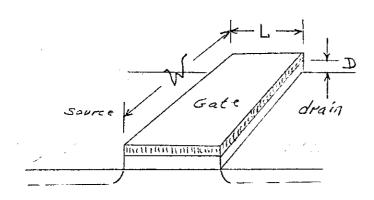
$$C \propto LW/D, \quad C'/C = (L/\alpha)(W/\alpha)/(D/\alpha)]/[LW/D], \quad \therefore \quad C' = C/\alpha$$

$$I \propto WV^2/LD, \quad I'/I = [(WV^2/\alpha^3)/(LD/\alpha^2)]/[WV^2/LD], \quad \therefore \quad I' = I/\alpha$$

Switching power,  $P_{SW}$ , is the energy stored on the capacitance of a given device divided by the clock period, or time between successive charging and discharging of the capacitance. A system's clock period is proportional to the  $\tau$  of its smallest devices. As devices are made smaller and faster, the clock period is proportionally shortened. Also, the dc power,  $P_{dc}$ , dissipated by any static circuit equals 1 times V. Therefore,

$$P_{sw} \propto CV^2/\tau \propto WV^3/DL$$
,  $P_{sw} = P_{sw}/\alpha^2$   
 $P_{dc} = IV$ ,  $P_{dc} = P_{dc}/\alpha^2$ 

Both the switching power and static power per device scale down as  $1/\alpha^2$ . The average dc power for most systems can be approximated by adding the total  $P_{SW}$  to one-half the total dc power which would result if all level restoring logic pulldowns were turned on. The contribution of pass transistor logic to the average dc power drawn by the system is due to



W:Wb L=L/d

W:Wb + D'= D/d

Fig. 14a. MOSFET, 1977

Fig. 14b. MOSFET SCALED

DOWN by X, 19xx

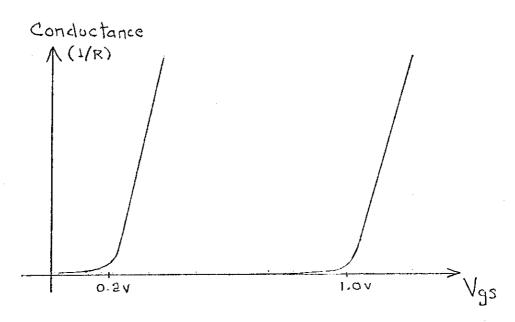


Fig. 15 Conductance as a Function of Threshold Voltage

the switching power consumed by the driving circuits which charge and discharge the pass transistor control gates.

The power-delay product at maximum clock frequency, an important metric of device performance, equals the switching energy per device  $E_{SW}$  and scales down as follows:

$$E_{sw} \propto CV^2$$
,  $E_{sw}' = E_{sw}/\alpha^3$ 

A more detailed plot of the channel conductance of an MOS transistor near the threshold voltage is shown in figure 15. Below the nominal threshold, the conductance (1/R) is not in reality zero, but depends on gate voltage and temperature as follows:

$$1/R \propto e^{(V_{gs}-V_{th})/(kT/q)}$$

where T is the absolute temperature, q is the charge on the electron, and k is Boltzmann's constant. At room temperature,  $kT/q \sim 0.025$  volts. At present threshold voltages, as in the right curve in figure 15., an off device is below threshold by perhaps 20 kT/q, i.e. by about 0.5 volts, and its conductance is decreased by a factor of the order of ten million. Said another way, if the device is used as a pass transistor, a quantity of charge which takes a time  $\tau$  to pass through the on device, will take a time on the order of  $10^7\tau$  to "leak" through the off device. The use of pass transistors switches to isolate and "dynamically store" charge on circuit nodes is common in many memory applications using 1977 transistor dimensions. However, if the threshold voltage is scaled down by a factor of perhaps 5, as shown in the left plot in figure 15., then an off transistor is only 4kT/q below threshold. Therefore its conductance when "off" is only a factor of 100 or so less than when it is "on". Charge stored dynamically on a circuit node by the transistor when "on", will safely remain on that node for only a few typical system clock periods. The charge will not remain on the node for a very large number of periods as in present memory devices using this technique.

Now, suppose we scale down an entire LSI system by a scale down factor of ten. The resulting system will have one hundred times the number of circuits per unit area. The total power per unit area remains constant. All voltages are reduced by the factor of ten. The current per unit area is increased by a factor of ten. The time delay per stage is decreased by a factor of ten. The power-delay product decreases by a factor of one thousand.

This is a rather attractive scaling in all ways except for the current density. The delivery of

the required average dc current presents an important obstacle to scaling. This current must be carried to the various circuits in the system on metal level paths, in order that the voltage drop from the offchip source to the onchip subsystems will not be excessive. Metal paths have an upper current density limit imposed by a phenomenon called metal migration, discussed further in chapter 2. Many metal paths in today's integrated circuits are already operated near their current density limit. As the above type of scaling is applied to a system, the conductors get narrower, but still deliver the same current on the average to the circuits supplied by them.

Therefore, it will be necessary to find ways of decreasing system current requirements to approximately a constant current per unit area relative to the present current densities. In n-channel silicon gate technology, this objective can be partially achieved by using pass transistor logic in as many places as possible and avoiding restoring logic except where it is absolutely necessary. Numerous examples of this sort of design are given in this text. This design approach also has the advantages of tending to minimize delay per unit function and to maximize logic functions per unit area. However, when scaled down to submicron size, the pass transistors will suffer from the subthreshold current problem. It is possible that when the fabrication technologies have been developed to enable scaling down to submicron devices, a technology such as complementary MOS, which does not draw any decurrent, may be preferable to the nMOS technology used to illustrate this monograph. However, even if this occurs, the methodology developed in the text can still be applied in the design of integrated systems in that technology.

The limit to this kind of scaling occurs when the devices created are no longer able to perform the switching function. To perform the switching function, the ratio of transistor on to off conductance must be >>1, and therefore the voltage operating the circuit must be many kT/q. For this reason, even circuits optimized for operation at the lowest possible supply voltages still require a VDD of ~ 0.5 volts. 1977 devices operate with a VDD of approximately five volts and minimum channel lengths of approximately five microns. Therefore, the kind of scaling we have envisioned here will take us to devices with approximately one half micron channel lengths and current densities approximately ten times what they are today. Power per unit area will remain constant over that range. Smaller devices might be built but must be used without lowering the voltage any further. Consequently the power per unit area will increase. Finally, there appears to be a fundamental limit of approximately one quarter micron channel length, where certain physical effects such as the tunneling through the gate oxide, and fluctuations in the

positions of impurities in the depletion layers, begin to make the devices of smaller dimension unworkable.

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## Reading References

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- R3. R. W. Keyes, "Physical Limits in Digital Electronics", *Proceedings of the IEEE*, Vol. 63, No. 5, May 1975, pp. 740-767, is an excellent invited survey paper on this topic.